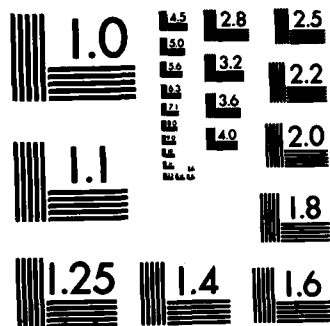


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A FORTRAN PROGRAM FOR THE LEVEL PROBABILITIES
OF ORDER RESTRICTED INFERENCE

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The University of Iowa
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Key words: Order restricted inference, level probabilities, chi-bar-square distribution.

LANGUAGE

Fortran

DESCRIPTION AND PURPOSES

↙ The level probabilities of order restricted inference are fundamental to that theory; their values are the probabilities that the order restricted, maximum likelihood estimates of normal means assume specified numbers of distinct values, called levels. Those probabilities are computed under the assumptions that the population means are equal and that the sampling from the various populations is done independently. The level probabilities depend upon a vector of weights (usually the various sample sizes) and the use of much of the theory of order restricted inference has been limited by the fact that those level probabilities can be virtually impossible to compute if the weights are not all equal.

Bohrer and Chow (1978; Algorithm AS 122) ↗ give a program for computing

these level probabilities when the number, K , of populations is no more than 10. Their program uses an algorithm for computing orthant probabilities which is due to Milton (1972). The time needed to use Milton's algorithm increases exponentially in K and can require several minutes or more of computation when $K \geq 6$ (cf. Bohrer and Chow).

Cran (1981; Algorithm AS 158) gives a program for computing these level probabilities when the number K does not exceed 6. For $K = 5$ it uses an approximation due to Plackett (1954) and for $K = 6$ an approximation due to Childs (1967) is used.

Robertson and Wright (1982) develop an approximation which is based upon an idea of Chase (1974) and uses the pattern of large and small weights. We refer the interested reader to Robertson and Wright (1982) for an evaluation of the quality of this approximation. The Fortran program given below uses this approximation for the values of the level probabilities for K such that $K \geq 6$. For $K \leq 20$ and equal weights or for general weights and $K \leq 5$ the program is identical to Cran's (1981; Algorithm AS 158).

STRUCTURE

SUBROUTINE PROBS (K, W, P, IFAULT)

K	Integer	input: the number of weights
W	Real Array (K)	input: the original weights
P	Real Array (K)	output: the computed probabilities
IFAULT	Integer	output: a fault indicator, equal to
		1 if at least one weight is not positive
		2 if $K < 2$ or $K > 20$
		3 if an error occurred in function FACT
		0 otherwise

Auxiliary Algorithms

FUNCTION PR1(I,J,W) computes explicitly the probabilities for $K \leq 5$.

(Algorithm AS 158.1)

FUNCTION F1(V1,V2,V3) computes the correlation $\rho = \left(\frac{V1 * V3}{(V1+V2)(V2+V3)} \right)^{-1/2}$.

(Algorithm AS 158.2)

FUNCTION FACT(M,IFAULT) computes n factorial. (Algorithm AS 158.5)

SUBROUTINE CHASE(K,CH,P1) computes the equal weight probabilities and Chase's approximations for a given K.

SUBROUTINE PAPRX(K,W,PA,CH,P1) computes the approximate probabilities:

K	Integer	input: the number of weights
W	Real Array(K)	input: the original weights
PA	Real Array(K)	output: the approximate probabilities
CH	Real Array(K,K)	input: Chase's approximate probabilities
P1	Real Array(K,K)	input: equal weight probabilities

Restrictions

The weight array can have no more than 20 elements, so $K \leq 20$. In addition, all weights must be positive.

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DIMENSION P(20), W(20)

5

DIMENSION P(20), W(20)

DRIVER PROGRAM FOR SUBROUTINE PROBS.

READ(5, 10) K

FORMAT(I2)

READ(5, 20) (W(I), I = 1, K)

FORMAT(10F8.4)

FCHEK CHECK THE INPUT VALUES.

WRITE(6, 30)

FORMAT(1H1)

WRITE(6, 40) K

FORMAT(4X, 10HTHERE ARE , I2, 5HWIGHTS.)

WRITE(6, 50)

FORMAT(4X, 15HTHE WRIGHTS ARE)

WRITE(6, 60) (W(I), I = 1, K)

FORMAT(4X, 10F12.7)

CALL PROBS(K, W, P, IFAULT)

IF (IFAULT .EQ. 1) GOTO 100

IF (IFAULT .EQ. 2) GOTO 120

IF (IFAULT .EQ. 3) GOTO 140

OUTPUT THE COMPUTED PROBABILITIES.

WRITE(6, 70)

FORMAT(//4X, 30HTHE COMPUTED PROBABILITIES ARE, /)

DO 90 L = 1, K

WRITE(6, 80) L, K P(L)

FORMAT(4X, 2HP(, I2, 1H, , I2, 4H) = , F10.7)

CONTINUE

STOP

WRITE(6, 110)

FORMAT(4X, 35HAT LEAST ONE WEIGHT IS NOT POSITIVE)

STOP

WRITE(6, 130)

FORMAT(4X, 17HK IS OUT OF RANGE)

STOP

WRITE(6, 150)

FORMAT(4X, 34HAN ERROR OCCURRED IN FUNCTION FACT)

STOP

END

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SUBROUTINE PROBS(K, W, P, IFAULT)

6

SUBROUTINE PROBS(K, W, P, IFAULT)

CALCULATION OF THE PROBABILITIES P(L,K) FOR
THE CASE OF SIMPLE ORDER.

DIMENSION L(20), P(20), Q(20, 20), CH(20, 20)
DIMENSION PR1(20, 20), PA(20, 20)
DATA C1/ 1.0E-6 /

CHECK THAT WEIGHTS ARE POSITIVE.

IF AULT = 0
DO 1 I = 1, K
IF (W(I) .LE. 0.0) GO TO 101
CONTINUE

CHECK THAT K .GE. 3 AND .LE. 20

IF (K .LT. 3 .OR. K .GT. 20) GO TO 102
WM = W(1)
DO 2 I = 2, K
IF (ABS(WM - W(I)) .GT. C1) GO TO 7
CONTINUE

EQUAL WEIGHTS

Q(1, 1) = 1.0 / 3.0
Q(2, 1) = 0.5
Q(3, 1) = 1.0 / 6.0
IF (K .EQ. 3) GO TO 5
DO 4 J = 4, K
AJ = J
A1 = 1.0 / AJ
A2 = (AJ - 1.0) * A1
Q(1, J) = A1
J1 = J - 1
DO 3 L = 2, J1
L1 = L - 1
Q(L, J) = A1 * Q(L1, J1) + A2 * Q(L, J1)
CONTINUE
Q(J, 1) = 1.0 / FACT(J, IFAULT)
IF(IFAULT .NE. 0) RETURN
CONTINUE
CONTINUE
DO 6 J = 1, K
P(J) = Q(J, K)
CONTINUE
RETURN

UNEQUAL WEIGHTS - CHECK THAT K .LE. 6

IF (K .GT. 6) GO TO 11
K2 = K - 2
GO TO (8, 9, 10), K2
P(1) = PR1(1, 3, W)
P(2) = 0.5
P(3) = 0.5 - P(1)
RETURN
P(1) = PR1(1, 4, W)
P(4) = PR1(4, 4, W)

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P( 2 ) = 0.5 - P( 4 )
P( 3 ) = 0.5 - P( 1 )
RETURN
10 P( 5 ) = PR1( 5, 5, W )
P( 4 ) = PR1( 4, 5, W )
P( 2 ) = 0.5 - P( 4 )
P( 1 ) = PR1( 1, 5, W )
P( 3 ) = 0.5 - P( 1 ) - P( 5 )
RETURN
11 CALL CHASE( K, CH, P1 )
CALL PAPRX( K, W, PA, CH, P1 )
DO 12 J = 1, K
P( J ) = PA( J, K )
12 CONTINUE
RETURN
101 IFAULT = 1
RETURN
102 IFAULT = 2
RETURN
END
C
C FUNCTION PR1( I, J, W )
C
C     ALGORITHM AS 158.1, APPL STAT ( 1981 ), VOL 30, NO 1
C
C     EXPLICIT CALCULATION OF PROBABILITIES FOR K .LE. 5
C     ALSO CALLED BY FUNCTION F2
C
C DIMENSION W( 10 )
C DATA P11/ 0.318309886 /
C IF ( J .NE. 3 ) GO TO 40
C = 0.5 + P11 + F1( W( 1 ), W( 2 ), W( 3 ) )
C IF ( I .EQ. 3 ) GO TO 30
PR1 = 0.25 - C
RETURN
30 PR1 = 0.25 + C
RETURN
40 W1 = W( 1 )
W2 = W( 2 )
W3 = W( 3 )
W4 = W( 4 )
W12 = W1 + W2
W23 = W2 + W3
W34 = W3 + W4
S12 = F1( W1, W2, W3 )
S23 = F1( W2, W3, W4 )
IF ( J .EQ. 5 ) GO TO 50
IF ( I .EQ. 4 ) GO TO 41
C1 = 0.25 + P11 +
* ( F1( W1, W2, W34 ) + F1( W1, W23, W4 ) + F1( W12, W3, W4 ) )
PR1 = 0.125 - C1
RETURN
41 C2 = 0.25 + P11 + ( S12 + S23 )
PR1 = 0.125 + C2
RETURN
50 W5 = W( 5 )
W45 = W4 + W5
W123 = W12 + W3
W234 = W23 + W4
W345 = W34 + W5

```

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S34 = F1( W3, W4, W5 )
IF ( I.EQ. 4 ) GO TO 52
C5 = 0.0625 + 0.125 * PII * ( S12 + S23 + S34 ) +
* 0.25 * PII * S12 * S34

```

```

IF ( I.EQ. 1 ) GO TO 51
PR1 = C5
IF ( PR1.LT. 0.0 ) PR1 = 0.0
RETURN

```

```

51 S113 = F1( W1, W2, W345 )
S131 = F1( W1, W234, W5 )
S311 = F1( W123, W4, W5 )
C3 = 0.375 + 0.125 * PII * ( S113 + S131 + S311 + F1(W1, W23, W45)
* + F1(W12, W3, W45) + F1(W12, W34, W5) - S12 - S23 - S34 )
* - 0.25 * PII * PII * ( S12 + S311 + S23 + S131 + S34 + S113 )
PR1 = 0.5 - C3 - C5
RETURN

```

```

52 C2 = 0.125 * PII * ( S12 + S34 + F1(W1, W2, W34) + F1(W12, W3, W4)
* + F1(W1, W23, W4) + F1(W2, W3, W45) + F1( W23, W4, W5 ) +
* F1(W3, W34, W5 ) )
PR1 = 0.25 + C2
RETURN
END

```

```

FUNCTION F1( V1, V2, V3 )

```

```

ALGORITHM AS 158.2 APPL STAT (1981) VOL 30, NO 1

```

```

RHO = -SQRT( V1 * V3 / ( ( V1 + V2 ) * ( V2 + V3 ) ) )
F1 = ASIN( RHO )
RETURN
END

```

```

FUNCTION FACT( M, IFAULT )

```

```

ALGORITHM AS 159.5 APPL STAT ( 1981 ) VOL 30, NO 1

```

```

CALCULATION OF M FACTORIAL

```

```

DATA MAXM/ 50 /
IFault = 0
IF ( M.LT. 0 .OR. M.GT. MAXM ) RETURN
IFault = 0
FACT = 1.0
IF ( M.LE. 1 ) RETURN
A1 = 1.0
DO 1 I = 2, M
A1 = I
1 CONTINUE
FACT = A1
RETURN
END

```

```

FUNCTION ASIN( X )
ASIN = ATAN( X / SQRT( 1.0 - X*X ) )
RETURN
END

```

```

SUBROUTINE CHASE(K, C4, P )

```

```

THIS SUBROUTINE COMPUTES CHASE'S AND EQUAL WEIGHTS
PLK'S.

```

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SUBROUTINE PROPS(K, W, P, IFAULT)

9

REAL CH(20,20),P(20,20)

INITIALIZE MATRICES TO ZERO.

DO 20 J = 1, 20

DO 10 I = 1, 20

CH(I,J) = 0.0

P(I,J) = 0.0

CONTINUE

CONTINUE

CH(1,1) = 1.0

CH(1,2) = 0.5

CH(2,2) = 0.5

P(1,1) = 1.0

P(1,2) = 0.5

P(2,2) = 0.5

DO 40 J = 2, K

J1 = J + 1

X = 2 * J - 1

Y = 2 * J

U = J

V = J + 1

CH(1,J1) = X / Y * CH(1,J)

CH(J1,J1) = 1.0 / Y * CH(J,J)

P(1,J1) = U / V * P(1,J)

P(J1,J1) = 1.0 / V * P(J,J)

DO 30 I = 2, J

IA = I - 1

CH(I,J1) = (1.0 / Y) * CH(IA,J) + (X / Y) * CH(I,J)

P(I,J1) = (1.0 / V) * P(IA,J) + (U / V) * P(I,J)

CONTINUE

CONTINUE

RETURN

END

SUBROUTINE PAPRY(K, W, PA, CH, P)

THIS SUBROUTINE COMPUTES THE APPROXIMATE PLK'S

REAL W(20),PA(20,20),PB(20,20),PRP(20,20),CH(20,20),P(20,20)

INTEGER INDEX(20),A,B

ALPHA = 1.0 / 3.0

INITIALIZE PA,PB,PRP

DO 20 J = 1, 20

DO 10 I = 1, 20

PA(I,J) = 0.0

PB(I,J) = 0.0

PRP(I,J) = 0.0

CONTINUE

CONTINUE

DETERMINE MAXIMUM AND MINIMUM OF WEIGHTS.

WMAX = W(1)

WMIN = W(1)

DO 25 I = 2, K

IF (W(I) .LT. WMIN) WMIN = W(I)

IF (W(I) .GT. WMAX) WMAX = W(I)

CONTINUE

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CUT = 0.65 * WMIN + 0.35 * WMAX

DETERMINE THE INDICES OF THE WEIGHTS

DO 40 I = 1, K
 IF (W(I) .LT. CUT) GOTO 30
 INDEX(I) = 1
 GOTO 40
 30 INDEX(I) = 0
 CONTINUE

COMPUTE THE NUMBER OF LARGE WTS

M = 0
 DO 50 I = 1, K
 M = M + INDEX(I)
 50 CONTINUE

IF ALL WTS LARGE OR SMALL SET PA=P

IF ((M.EQ.0).AND.(K.NE.K)) GO TO 70
 DO 60 L = 1, K
 PA(L,K) = P(L,K)
 60 CONTINUE
 GO TO 270

IF A=0 AND P=0 SET PB=PLM

N = INDEX(1) + INDEX(K)
 IF (N.NE.0) GO TO 90
 DO 80 L = 1, M
 PB(L,K) = P(L,M)
 80 CONTINUE
 GO TO 240

DETERMINE A,P

90 A = 0
 B = 0
 DO 100 I = 1, K
 IF (INDEX(I) .NE. 0) GO TO 110
 A = A + 1
 100 CONTINUE
 110 DO 120 I = 1, K
 J = K - I + 1
 IF (INDEX(J) .NE. 0) GO TO 130
 B = B + 1
 120 CONTINUE
 130 N1 = A + 1
 N2 = B + 1
 IF (A .NE. 0) GO TO 140
 DO 150 L = 1, K
 SUM = 0.0
 DO 140 I = 1, L
 J = L - I + 1
 SUM = SUM + P(I,M) + PB(J,K)
 140 CONTINUE
 PB(L,K) = SUM
 150 CONTINUE
 GO TO 240

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```

160  IF (P.EQ.0) GO TO 190
    DO 180 L = 1, K
      SUM = 0.0
      DO 170 I = 1, L
        J = L - I + 1
        SUM = SUM + P(I,M) * CH(J,N1)
170  CONTINUE
      PB(L,K) = SUM
180  CONTINUE
    GO TO 190
190  DO 210 L = 1, K
      SUM = 0.0
      DO 200 I = 1, L
        J = L - I + 1
        SUM = SUM + CH(I,N1) * CH(J,N2)
200  CONTINUE
      PRP(L,K) = SUM
210  CONTINUE
      DO 230 L = 1, K
        SUM = 0.0
        DO 220 I = 1, L
          J = L - I + 1
          SUM = SUM + PRP(I,K) * P(J,M)
220  CONTINUE
        PB(L,K) = SUM
230  CONTINUE
C
C  DETERMINE R
C
240  SUM1 = 0.0
      SUM2 = 0.0
      DO 250 I = 1, K
        X = INDEX(I)
        Y = 1 - INDEX(I)
        SUM1 = SUM1 + W(I) * X
        SUM2 = SUM2 + W(I) * Y
250  CONTINUE
      X = K - M
      Y = M
      R = (SUM1 * X) / (SUM2 * Y)
      DO 260 L = 1, K
        PA(L,K) = (1. - (1.0)/(R**ALPHA)) * PB(L,K) + ((1.0)/(R**ALPHA)) * P(L,K)
260  CONTINUE
270  RETURN
    END

```

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